Asymptotically Optimal Simple User Scheduling for Massive MIMO Downlink with Two-Stage Beamforming

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I. INTRODUCTION

The massive MIMO technology is considered as one of the core technologies for next generation wireless communication. However, there are several challenges to realize the potential of massive MIMO in real world engineering. Practical precoding architecture design for massive MU-MIMO downlink is one of such challenges. Designing precoding vectors or matrices with very high dimensions without introducing an efficient structure requires heavy complexity. One feasible precoding solution to multi-user massive MIMO downlink is two-stage beamforming. Recently, Adhikary et al. proposed an efficient two-stage beamforming method named ‘Joint Spatial Division and Multiplexing (JSDM)’ for multi-user massive MIMO downlink [2]. The main ideas of JSDM are 1) to partition users in a cell into groups each of which has a distinguishable linear subspace spanned by the dominant eigenvectors of the group’s channel covariance matrix and 2) to divide transmit beamforming into two stages: pre-beamforming that separates groups by designing a pre-beamforming matrix for each group filtering the dominant eigenvectors of each group’s channel covariance matrix and following MU-MIMO precoding that separates the users within a group based on the effective channel formed as the product of the pre-beamforming matrix and the actual channel matrix. One major advantage of such two-stage beamforming is that the pre-beamforming matrices can be designed without much difficulty since the channel covariance matrix of a user terminal (UT) changes slowly compared with the CSI and can be estimated without knowing instantaneous CSI. Furthermore, the channel covariance matrix in a realistic environment has a much smaller rank than the size of the original physical channel and hence the dimension of the effective channel (whose state information should be acquired) is significantly reduced and conventional MU-MIMO techniques such as zero-forcing (ZF) or minimum mean-square error (MMSE) beamforming based on effective CSI can be applied to the second-stage beamforming of JSDM.

In this paper, we consider optimal user scheduling for such two-stage beamforming and propose a simple but asymptotically optimal user scheduling method for such two-stage beamforming. User scheduling based on beamforming or opportunistic beamforming for MU-MIMO systems has been investigated extensively for the past decade [3]–[7]. For example, two representative user selection schemes were proposed under random beamforming (RBF) [3] and ZFBF [5] for uncorrelated channels. Both schemes, [3] and [5], are asymptotically optimal but have significantly different performance in the practical case of finite users due to the difference in the amount of feedback required for user selection. Since the user selection scheme in [5], named ‘semi-orthogonal user selection (SUS)’, exploits full CSI from all users, a smart selection of beamforming directions is possible and SUS has fairly good performance under the ZFBF strategy. On the other hand, the RBF scheme in [3] chooses a group of users to be nearly matched to predetermined random beam directions, and requires only the feedback of the best beam direction index and the corresponding SINR value from each user. Thus, the feedback overhead can be reduced significantly for the RBF scheme. Due to such feedback advantage, the RBF scheme was extended to the single correlated channel case [6] and recently to JSDM with multiple correlated channel groups [7]. However, as we shall see in Section V, the RBF scheme shows poor performance in the practical case of finite users. In this paper, we propose a new simple user scheduling method for JSDM with multiple correlated channel groups that overcomes the disadvantages of SUS and RBF. The proposed method is asymptotically optimal and shows good performance with significantly reduced feedback overhead.

Abstract—In this paper, a simple user-scheduling-and-beamforming method is proposed for massive multi-user multiple-input multiple-output (MU-MIMO) downlink adopting two-stage beamforming. The key ideas of the proposed scheduling-and-beamforming method are to divide users into several candidate subsets according to the level of alignment of user channels to the dominant directions of the channel covariance matrix and select the user in each candidate subset based on a certain channel quality indicator (CQI) and to apply post-selection zero-forcing beamforming (ZFBF) to the selected users based on their channel state information (CSI). It is proved that the proposed scheduling-and-beamforming method is asymptotically optimal as the number of users increases. Furthermore, the proposed method significantly reduces the feedback overhead and shows superior sum rate performance compared to existing scheduling methods for MU-MIMO downlink.

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II. System Model and Preliminaries

We consider a single-cell MIMO downlink system consisting of a single base station (BS) employing $M$ transmit antennas and $K$ single-antenna UTs. We consider the large-number-of-users regime, i.e., $K \gg M$, and assume that the BS chooses $S \leq M$ users among the $K$ users within the cell and broadcasts independent data streams to the BS chooses $S$ number-of-users regime, i.e., $K\leq S$, and the BS knows its effective channel $G_g = [w_{1g}, \cdots, w_{Kg}]$, downlink MU-MIMO precoder $W_g$ of group $g$, respectively. Let the row-wise decomposition of $G_g$ and the column-wise decomposition of $W_g$ be $G_g = [g_{1g}, \cdots, g_{Kg}]^H$ and $W_g = [w_{1g}, \cdots, w_{Kg}]$, respectively. Then, the received signal of user $k$ in group $g$ is given by

$$y_k = G_g W_g d_k + \sum_{g' \neq g} H_{g'} V_{g'} W_{g'} d_{g'} + n_{g_k},$$

where $d_k$ and $n_{g_k}$ are the data and noise vectors for group $g$, respectively.

Regarding the inter-user interference, we assume that at least the approximate block diagonalization (BD) condition holds: [2]

- Exact BD: Each group has a sufficient signal space to transmit $S_g$ multiple data streams that does not interfere with other groups, i.e., [2]

$$\dim(\text{span}(U_{g'})) \cap \text{span}^\perp(\{U_{g'} : g' \neq g\}) \geq S_g.$$  

- Approximate BD: When exact BD is not possible, approximate BD can be achieved by selecting a matrix $\mathbf{U}_{g}^{*}$ composed of the $r_{g}^\ast$ ($\geq r_{g}$) dominant eigenvectors for each group $g$ such that $r_{g}^\ast$ is a control parameter [2]

$$\dim(\text{span}(\mathbf{U}_{g}^{*})) \cap \text{span}^\perp(\{U_{g'} : g' \neq g\}) \geq S_g.$$  

Note that in the case of approximate BD, the inter-group interference still remains in (5) due to the weakest $r_{g} - r_{g}^\ast$ eigenvectors not included in $\{U_{g'}\}$. Note that both $U_g$ and $\mathbf{U}_{g}^{*}$ have column-wise submatrices of a unitary matrix. Thus, the average transmit power for user $g_k$ is $\|w_{g_k}\|^2$ when $V_g = \mathbf{U}_{g}^{*}$.

III. The Proposed User Scheduling Algorithm

In this section, we propose a user scheduling algorithm for a given pre-beamformer $V = [V_1, \cdots, V_G]$ in the two-stage MU-MIMO precoder $W_g$. In this algorithm, we assume that $g_{1g} = S_g = r_{g}^\ast$ and $V_g = \mathbf{U}_{g}^{*}$, $\forall g$. We also assume that each user $g_k$ (not BS) knows its effective CSI $g_{k0}$ and the power allocated to group $g$ is proportional to the number of supported users in group $g$.
The Proposed User Selection Method

0) \( \alpha \in (0, 1) \) is a pre-determined parameter and is shared by the BS and all UTs. The BS initializes

\[ \mathcal{W}_{g,i} = \emptyset, \text{ for } i = 1, \ldots, r^*_g \]  

(8)

\[ S_g = \emptyset. \]  

(9)

1) Each user \( g_k \) independently computes the following set:

\[ \mathcal{I}_{g_k} := \left\{ i : \left| e^H_{y,i} g_k \right| \geq \alpha, i = 1, \ldots, r^*_g \right\}, \]  

(10)

where \( e_{y,i} \) is the \( i \)-th column of \( I_r \).

If user \( g_k \) has \( \mathcal{I}_{g_k} \neq \emptyset \), then the user finds

\[ i^*_g = \arg \max_{i \in \mathcal{I}_{g_k}} \left| e^H_{y,i} g_k \right| \]  

(11)

and feedbacks the pair \((i^*_g, R(g_k))\) to the BS, where

\[ R(g_k) := \frac{1}{\| g_k \|^2} \sum_{g' \neq g} \| h^H_{g'} W_{g'} \|^2 \]  

(12)

where \( \rho := \frac{\rho}{\| g_k \|^2} \). If \( \mathcal{I}_{g_k} = \emptyset \), user \( g_k \) does not feedback.

After the feedback, the BS updates \( W_{g_i}, i \subseteq \mathcal{W}_{g_i} \) and stores \( R(g_k) \).

2) For \( i = 1, \ldots, r^*_g \), the BS finds

\[ \kappa_{g,i} = \arg \max_{k \in \mathcal{W}_{g,i}} R(g_k), \]  

(13)

and updates

\[ S_g \leftarrow S_g \cup \{ \kappa_{g,i} \}. \]  

(14)

3) The BS transmits a paging signal to notify that the users in \( S_g \) are scheduled and then, the corresponding UTs feedback their effective CSI to the BS. Finally, the BS constructs the MU-MIMO ZFBF precoder with water-filling power allocation for each group and transmits data streams to the scheduled UTs.

In step 1), each user checks the level of alignment of its channel to each of the \( r^*_g \) dominant channel directions in \( U^g_{\alpha} \) of group \( g \) by computing (10). (Note that \( g_k = [h^H_{g_k} u^i_{g_k}, \ldots, h^H_{g_k} u^i_{g_k}]^H \), where \( u^i_{g_k} \) is the \( i \)-th column of \( U^g_{\alpha} \).) If \( g_k \) has a non-empty set \( \mathcal{I}_{g_k} \) of channel directions of alignment level \( \alpha \), then user \( g_k \) finds the most aligned direction in \( \mathcal{I}_{g_k} \) and feedbacks the direction index \( i^*_g \) and the quasi-SINR \( R(g_k) \) to the BS. If \( \mathcal{I}_{g_k} = \emptyset \), then user \( g_k \) does not feedback any information to the BS.

After the quasi-SINR feedback period is over, the BS makes \( r^*_g \) candidate sets \( \{ \mathcal{W}_{g,i} \} \) for \( r^*_g \) channel directions for group \( g \), based on the feedback information. Here, \( \mathcal{W}_{g,i} \) represents the set of users whose channels are most aligned to the \( i \)-th dominant direction of \( U^g_{\alpha} \) with level larger than or equal to \( \alpha \). In step 2), the BS chooses the user \( \kappa_{g,i} \) having the largest quasi-SINR \( R(g_k) \) in each set \( \mathcal{W}_{g,i}, i = 1, \ldots, r^*_g \), to construct the set \( S_g \) of scheduled users for each group \( g \). As explained in [1], by the use of (10) with the threshold \( \alpha \) and the quasi-SINR (12), we can select semi-orthogonal users with large channel magnitude as the SUS algorithm in [5].

Step 3) is a beam construction stage based on ZFBF after the selection of semi-orthogonal users with large channel magnitude by steps 1) and 2). Step 3) requires CSI feedback only from the selected users not from all users.

Remark 2. As seen, the proposed method is composed of two steps: The first is the user selection step based on scalar-valued quasi-SINR feedback and the second step is the ZFBF beam construction and data transmission to the selected users based on CSI feedback from the selected users. The amount of feedback required for the proposed method for group \( g \) is \( \sum_{i=1}^{r^*_g} |W_{g,i}| \) integers (for user index feedback) and \( \sum_{i=1}^{r^*_g} |W_{g,i}| + 2(r^*_g)^2 \) real numbers (for quasi-SINR feedback and later effective CSI feedback). Note that only \( r^*_g \) users per group need to feedback their effective CSI of (complex) dimension \( r^*_g \) for one scheduling period for the proposed scheme. It can be shown that when \( \alpha \leq 1/\sqrt{r^*_g} \), \( \mathcal{I}_{g_k} = \emptyset \) is a non-empty set for all \( g_k \) and thus, every user feedbacks its quasi-SINR to the BS. Hence, in this case, \( \sum_{i=1}^{r^*_g} |W_{g,i}| \) reduces to \( K_g \). When \( \alpha > 1/\sqrt{r^*_g} \), on the other hand, \( \mathcal{I}_{g_k} = \emptyset \) for some users and thus in this case, \( \sum_{i=1}^{r^*_g} |W_{g,i}| \) can be less than \( K_g \).

In Section V, numerical results show that many users does not feedback to the BS for optimally chosen \( \alpha \). Hence, the feedback overhead can be reduced drastically.

IV. Optimality of the Proposed Method

In this section, we prove the asymptotical optimality of the proposed method as \( K \rightarrow \infty \). We start with the optimal capacity scaling law for the general \( K \)-user MISO broadcast channel consisting of multiple groups with each group’s having the same channel covariance matrix.

Theorem 1: [7] In a MU-MISO downlink system consisting of a BS with \( M \) antennas and total power constraint \( P \) and \( K \) single-antenna users divided into \( G \) groups of equal size \( K' = K/G \), where the channel vector of each user in group \( g \) is independent and identically distributed (i.i.d.) from \( \mathcal{CN}(0, R_g) \) for \( g = 1, \ldots, G \), the sum-rate capacity (which is achieved by DPC) scales as

\[ R_{DPC} = \beta \log \left( \log (K') \right) + \beta \log \frac{P}{\beta} + O(1) \]  

(15)

where \( \beta = \min \left\{ M, \frac{\sum_{g=1}^{G} r_g}{G} \right\} \) and \( O(1) \) denotes a constant, independent of \( K' \), as \( K' \rightarrow \infty \).

Proof: See Theorem 1 in [7].

The same scaling law is achieved by the proposed method under the approximate BD condition.

Theorem 2: In the system described in Theorem 1, the sum-rate of the scheduled sets \( \{S_g\} \) by the proposed method scales as

\[ \mathbb{E} \left[ \sum_{g=1}^{G} R_{ZF,g}(S_g) \right] \sim R_{DPC}, \]  

(16)
where \( x \sim y \) indicates that \( \lim \frac{x}{y} = 1 \). Here, \( R_{Z_{F},g}(S_g) \) is the sum-rate of the users in \( S_g \) determined by the proposed method with ZF MU-MIMO second-stage precoding.

Proof: Proof of the optimality is by showing both the effective channel gain reduction and the multi-user diversity gain reduction associated with the proposed method become negligible as \( K' \to \infty \).

1) Effective channel gain: Since ZFBF is assumed for the second-stage beamforming, we have \( W_g := W_g(S_g) = G^H(S_g)G(S_g)G^H(S_g) - P_i, \) and \( P_g = \text{diag}(\sqrt{\frac{1}{P_{g,i}}}, \ldots, \sqrt{\frac{1}{P_{g,j}}}) \), where \( P_{g,i} \) is the transmit power loading factor for the scheduled user \( g,i \in S_g \). (Since the pseudo-inverse \( G^H(S_g)(G(S_g)G^H(S_g))^{-1} \) is given for the given effective channel, we need \( P_g \) to control the user power.) Then, the effective channel gain \( \gamma_{g,i} \) for user \( g,i \) is given by [5]

\[
\gamma_{g,i} = \frac{1}{\|G(S_g)G(S_g)H\|_{i,i}} \tag{17}
\]

Since \( \|G(S_g)G(S_g)H\|_{i,i} \), we can decompose it as

\[
G(S_g)G(S_g)^H = D \Gamma G,
\]

where \( D = \text{diag}(\|g_{g,i,1}\|, \ldots, \|g_{g,i,r}\|) \) and

\[
\Gamma = \begin{bmatrix}
1 & \tilde{g}_{g,i,1}^H & \tilde{g}_{g,i,2}^H & \cdots & \tilde{g}_{g,i,r-1}^H & \tilde{g}_{g,i,r}^H \\
\tilde{g}_{g,i,1} & 1 & & & & \\
\tilde{g}_{g,i,2} & & 1 & & & \\
\vdots & & & 1 & & \\
\tilde{g}_{g,i,r-1} & & & & 1 & \\
\tilde{g}_{g,i,r} & & & & & 1
\end{bmatrix}
\]

with \( \tilde{g}_{g,i} = \frac{\tilde{g}_{g,i}}{\|g_{g,i}\|} \), \( \forall i \). Substituting (18) into (17), we have

\[
\gamma_{g,i} = \frac{1}{\|g_{g,i}\|^2/\|\Gamma^{-1}\|_{i,i}} \tag{20}
\]

First, consider the term \( \|\tilde{G}^{-1}\|_{i,i} \). Since \( \kappa_{g,i} \in W_{g,i} \), it is easy to show that \( \|\tilde{G}^{-1}\|_{i,i} \leq 2\alpha \sqrt{1 - \alpha^2} \) for \( i \neq j \) when \( \alpha > 1/\sqrt{2} \). By the Gershgorin circle theorem [9], every eigenvalue of the Hermitian matrix \( G \) is in a Gershgorin disk

\[
\lambda(G) \subseteq \{ z \in \mathbb{C} : |z - 1| \leq 1 \} \tag{21}
\]

where (a) follows from (21), and \( \lambda_{\min}(\tilde{G}) \) is the minimum eigenvalue of \( \tilde{G} \). Thus, from (20), the effective channel gain \( \gamma_{g,i} \) is lower bounded by

\[
\gamma_{g,i} > \frac{\|g_{g,i}\|^2}{1 - (r_g - 1)2\alpha \sqrt{1 - \alpha^2}} \tag{23}
\]

As \( K' \to \infty \), \( \alpha \) can be made arbitrarily close to 1 such that \( W_{g,i} \) is not empty for each \( i \) in group \( g \) since \( \sum_{i=1}^{K'} 2\alpha \sqrt{1 - \alpha^2} \) converges to one and \( \gamma_{g,i} \to \|g_{g,i}\|^2 \), i.e., there is no loss in the effective channel gain.

2) Multi-user diversity gain: Define

\[
\phi_{g,i} = \begin{cases} R(g_k), & k \in W_{g,i} \\ 0, & \text{Otherwise} \end{cases} \tag{24}
\]

for \( k = 1, \ldots, K_g \). Then, for a given \( i \), the random variable \( \phi_{g,i} \) is i.i.d. across \( k \) in the same group \( g \). Note that

\[
\gamma_{k,g} = \arg \max \{ R(g_k) \} = \arg \max \{ \phi_{g,i} \} \tag{25}
\]

The multi-user diversity gain results from choosing the best user among all users with i.i.d. channel realizations. However, with the proposed method, for each data stream, the best user within \( W_{g,i} \) is chosen, and thus there exists some loss in the multi-user diversity gain. However, for the proposed method, with the approximate BD condition we can show for each \( i \)

\[
\Pr(\phi_{g,i} > u_g) \geq 1 - O(1/K'), \tag{26}
\]

where \( u_g = (\lambda_{g,1} \log K' - \lambda_{g,1} \log \log K' + c)/(1/p + c) \), \( \lambda_{g,1} \) is the maximum eigenvalue of \( R_g \), and \( a_1 \) and \( c \) are constants independent of \( K' \). (Proof (25) is based on the extreme value theory applied to \( \phi_{g,i} \) and is omitted due to the lack of space. See [1] for detail.)

3) Finally, similarly to [5], (25) the general sum-rate formula for the ZF MU-MIMO broadcast channel consisting of users \( \{\kappa_{g,1}, \ldots, \kappa_{g,r}\} \) with power distribution \( \{P_{g,r_1}, \ldots, P_{g,r_g}\} \) can be derived as

\[
R_{Z_{F},g}(S_g) = \max_{\{P_{g,r_1}, \ldots, P_{g,r_g}\}} \sum_{i=1}^{r_g} \log \left( 1 + \frac{P_{g,r_i}}{\sum_{j \neq i} P_{g,r_j} \|g_{g,i}\|^2} \right) \tag{26}
\]

where \( \|w_{g,i}\|^2 = \gamma_{g,i} P_{g,i} \). Now, we show (16):

\[
E \left[ \sum_{g=1}^{K'} R_{Z_{F},g}(S_g) \right] \geq \sum_{g=1}^{K'} \sum_{i=1}^{r_g} \log \left( 1 + \frac{P_{g,r_i}}{\sum_{j \neq i} P_{g,r_j} \|g_{g,i}\|^2} \right) \tag{27}
\]

\[
E \left[ \sum_{g=1}^{K'} R_{Z_{F},g}(S_g) \right] \geq \sum_{g=1}^{K'} \sum_{i=1}^{r_g} \log \left( 1 + \frac{\|g_{g,i}\|^2}{\|g_{g,i}\|^2} \right) \tag{27}
\]

\[
E \left[ \sum_{g=1}^{K'} R_{Z_{F},g}(S_g) \right] \geq \sum_{g=1}^{K'} \sum_{i=1}^{r_g} \log \left( 1 + \frac{\|g_{g,i}\|^2}{\|g_{g,i}\|^2} \right) \tag{27}
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\]

\[
E \left[ \sum_{g=1}^{K'} R_{Z_{F},g}(S_g) \right] \geq \sum_{g=1}^{K'} \sum_{i=1}^{r_g} \log \left( 1 + \frac{\|g_{g,i}\|^2}{\|g_{g,i}\|^2} \right) \tag{27}
\]
where (a) follows from the suboptimal equal power allocation (simple equal power allocation for each data stream means \( \rho = \frac{1}{\sum_{g=1}^{G} r_g} = \| w_{k_g} \|^2 = \gamma_{k_g}^{-1} P_{k_g}, \forall g,i \)); (b) is obtained by (23) and submultiplicativity of norm; (c) holds by \( E_h(X) = \int_{-\infty}^{\infty} f(x)p(x)dx \geq Pr(X \geq u)f(u) \) for a monotone increasing function \( f \); (d) holds by (25); and (e) and (f) are obtained by simple manipulation. Hence, in both the cases of \( \Delta_k \) and \( \Delta \), each user is associated with the group \( g^* \) such that \( g^* = \arg \min_g \| U_k^H V^H g \|_2^2 \). After partitioning users into groups, we evaluated the sum rate performance (averaged over 20 iterations) of original SUS [5], RBF in [7], and the proposed method, as \( K_v \) varied, and the result is shown in Fig. 1. As shown in Fig. 1, the proposed method shows better performance than the two existing user scheduling methods: RBF and original SUS. Note that original SUS has a worse slope than the others. This is because SUS does not take inter-group interference into account. Thus, we modified SUS by using the metric in (12) to take the inter-group interference into account. As expected, the modified SUS shows the best performance since it exploits full CSI at the BS. The reason why RBF in [7] shows worse performance is explained in [1] in detail. Briefly speaking, there are mainly two reasons for the bad performance of RBF: the first is the metric used for RBF itself and the second is the lack of post-user-selection beam refinement. The two drawbacks of RBF were effectively corrected for the proposed method by using the metric (12) and applying post-user-selection ZFBF. Fig. 2 shows the amount of feedback (the number of real numbers) required for SUS, RBF, and the proposed method for the same setting as that for Fig. 1. The feedback overhead of the proposed method is far less than that of SUS and less than that of RBF.

V. NUMERICAL RESULTS

We evaluated the performance of the proposed method. We considered a MISO broadcast system where a BS was equipped with a ULA of \( M = 32 \) antenna elements and the covariance matrices of \( K \) UTs were modelled according to the one-ring model [2], [8]. Each user \( k \) had angle-of-arrival (AoA) \( \theta_{k} \), angle-spread (AS) \( \Delta_k \) and \( R_k \). We generated AoA and AS according to \( \theta_k \sim \text{Unif}[\pi/36, \pi/12] \) and \( \Delta_k \sim \text{Unif}[\pi/36, \pi/12] \) for each user independently. We set \( G = 8 \), \( b_g = r_g = b_y \geq S_g \), \( P = 15 \) [dB], and the pre-beamforming matrix \( V_g \) is the \( M \times b_y \) matrix such that \( V = [V_1, \ldots, V_G] \) is the \( M \times M \) DFT matrix [2], [8]. Each user \( k \) was associated with the group \( g^* \) such that \( g^* = \arg \min_g \| U_k^H V^H g \|_2^2 \). After partitioning users into groups, we evaluated the sum rate performance (averaged over 20 iterations) of original SUS [5], RBF in [7], and the proposed method, as \( K_v \) varied, and the result is shown in Fig. 1. As shown in Fig. 1, the proposed method shows better performance than the two existing user scheduling methods: RBF and original SUS. Note that original SUS has a worse slope than the others. This is because SUS does not take inter-group interference into account. Thus, we modified SUS by using the metric in (12) to take the inter-group interference into account. As expected, the modified SUS shows the best performance since it exploits full CSI at the BS. The reason why RBF in [7] shows worse performance is explained in [1] in detail. Briefly speaking, there are mainly two reasons for the bad performance of RBF: the first is the metric used for RBF itself and the second is the lack of post-user-selection beam refinement. The two drawbacks of RBF were effectively corrected for the proposed method by using the metric (12) and applying post-user-selection ZFBF. Fig. 2 shows the amount of feedback (the number of real numbers) required for SUS, RBF, and the proposed method for the same setting as that for Fig. 1. The feedback overhead of the proposed method is far less than that of SUS and less than that of RBF.

VI. CONCLUSION

In this paper, we have proposed an efficient user scheduling method for massive MIMO downlink systems. We have shown that the proposed method is asymptotically optimal and yields comparable performance of SUS (with the modified metric) and far better performance than RBF with feedback overhead less than RBF. Although the proposed method is derived for two-stage beamforming with multiple groups in a cell, the same method can be applied to single-stage conventional small-scale MU-MIMO too. Furthermore, the proposed method can easily be modified to implement fairness among users by adopting round-robin or proportional fairness principle.

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